

16 # Perpendicular + Parallel lines 10/7/15

Slope intercept $y = mx + b$

Standard form $Ax + By = C$
form

Parallel lines: since they never intersect
have the same slope

Perpendicular lines: intersect at a Right \angle
and have opposite reciprocal slope



Ex) $\frac{2}{3} \xrightarrow[\text{recip}]{\text{opp}} \frac{-3}{2}$

Ex) $5 \rightarrow \frac{-1}{5}$

Ex 1) Write an equation of a line that is parallel to $y = 3x - 5$ but goes through $(6, -2)$

Always

slope = 3
y-intercept =

$$\begin{aligned} y &= mx + b \\ -2 &= (3)(6) + b \\ -2 &= 18 + b \\ -18 & \quad -18 \\ -20 &= b \end{aligned}$$

use point to find new y-intercept

$$y = 3x - 20$$

Ex 2) Write an equation of a line that is perpendicular to $y = -4x + 2$ but goes through $(4, 5)$

Slope

$$m = \frac{1}{4}$$

y-intercept

$$y = \frac{1}{4}x + 4$$

$$\begin{aligned} y &= mx + b \\ 5 &= \frac{1}{4}(4) + b \\ 5 &= 1 + b \\ -1 & \quad -1 \\ 4 &= b \end{aligned}$$

Ex3) Write an equation of a line parallel to $2x + 3y = 9$ but going through $(18, -1)$

$$\begin{array}{r} 2x + 3y = 9 \\ -2x \quad -2x \\ \hline 3y = -2x + 9 \\ \frac{3y}{3} = \frac{-2x + 9}{3} \end{array}$$

$$y = \frac{-2}{3}x + 3$$

$$\rightarrow m = \frac{-2}{3}, (18, -1)$$

$$y = mx + b$$

$$-1 = \frac{-2}{3}(18) + b$$

$$-1 = -12 + b$$

$$11 = b$$

$$y = \frac{-2}{3}x + 11$$

Ex4) Solve for y

(A) $6x + 2y = 10$
 $2y = -6x + 10$

$$y = \frac{-6x + 10}{2}$$

$$y = -3x + 5$$

$$-y = +3x - 5$$

Vertical lines

$$x = ?$$

(B) $-2x - 21y = 14$
 $+2x \quad +2x$

$$-21y = \frac{2x + 14}{-21}$$

$$y = \frac{-2x}{21} + \frac{2}{3}$$

~~Vertical lines~~

Horizontal lines

$$y = ?$$

(C) $y + 10 = 2y$
 $y = 2x - 10$